

Total No. of Questions : 4]

SEAT No. :

P 850

ss[Total No. of Pages : 4

[5315]-450

T.Y. B.Sc.

STATISTICS (Principal)

ST - 344 : Operations Research

(2013 Pattern) (Paper - IV) (Semester - IV)

Time : 2 Hours]

[Max. Marks :40

Instructions to the candidates:

- 1) All questions are compulsory.
- 2) Figures to the right indicate full marks.
- 3) Use of scientific calculator is allowed.
- 4) Symbols and abbreviations have their usual meaning.

Q1) a) Choose the correct alternative in each of the following : **[1each]**

- i) If the primal linear programming problem (LPP) has infeasible solution, the solution of its dual is
 - 1) infeasible
 - 2) unbounded
 - 3) unique optimal
 - 4) not optimal
- ii) The method used for obtaining optimal solution of a Transportation Problem (TP) is
 - 1) Vogel's approximation method
 - 2) Least cost method
 - 3) Hungarian method
 - 4) Modified distribution (MODI) method
- iii) The solution to a TP with m sources and n destinations is non degenerate if the number of positive allocations is
 - 1) $m + n$
 - 2) $m + n - 1$
 - 3) $m \times n$
 - 4) $m + n + 1$

P.T.O

- iv) In PERT, variance of the project is based on
- 1) critical activities
 - 2) non - critical activities
 - 3) all activities
 - 4) dummy activities
- b) State whether each of the following is true or false. **[1each]**
- i) The dual of a dual is primal.
 - ii) Assignment problem can be treated as a particular case of transportation problem.
- c) Define each of the following. **[1each]**
- i) Artificial variable
 - ii) Surplus variable
- d) What is an unbalanced TP? How to convert it into a balanced TP? **[2]**

Q2) Attempt any two of the following : **[5 each]**

- a) A firm engaged in producing two models A and B performs three operations; assembly, painting and testing. The relevant data are as follows.

Total number of hours available each week are :

Assembly - 150 Painting - 80 Testing - 24

Model	Unit sale Price (in Rs.)	Hours Assembly	required for Painting	each unit Testing
A	50	1	0.5	0.2
B	80	1.25	0.5	0.1

The firm wishes to determine its weekly product - mix 50 as to maximize revenue. Formulate it as a LPP.

- b) Explain the following terms with regards to LPP.
- i) feasible solution
 - ii) optimal solution
 - iii) infeasible solution
 - iv) unbounded solution
 - v) alternate solution

c) Write dual of the following LPP

$$\begin{aligned} \text{Minimize } z &= 2x_1 + 3x_2 + x_3 \\ \text{Subject to } x_1 - x_2 + x_3 &\leq 5 \\ 2x_1 + x_2 &= 7 \\ x_1 + x_2 - x_3 &\geq 8 \\ x_1, x_2, x_3 &\geq 0 \end{aligned}$$

Q3) Attempt any two of the following :

[5 each]

- Explain the term "simulation". Write its merits and demerits.
- A car hire company has one car in each of four depots D_1, D_2, D_3 and D_4 . A Customer in each of four regions R_1, R_2, R_3 and R_4 requires a car. The distance in km between depots and regions is as follows.

Depo \ Region	R_1	R_2	R_3	R_4
D_1	160	120	50	55
D_2	130	120	50	35
D_3	190	160	80	80
D_4	200	175	110	105

How should cars be assigned to the customers so as to minimise the total distance travelled?

- Explain the following terms as regards to CPM :
 - earliest start time
 - earliest finish time
 - latest start time
 - latest finish time
 - critical path

Q4) Attempt any one of the following :

- a) i) Explain how simulation can be used to obtain probabilities of events related to gamma distribution. [3]
- ii) Following table gives per unit cost of transportation (in Rs.) from sources to destinations along with availability and requirement.

destination Sources	D ₁	D ₂	D ₃	D ₄	Availability
S ₁	15	10	17	18	20
S ₂	16	13	12	13	60
S ₃	12	17	20	11	70
Requirement	30	30	40	50	

Obtain IBFS using VAM. Further, find optimal solution. [7]

- b) i) Explain the following terms in PERT analysis [4]
- 1) Pessimistic time estimate
 - 2) Optimistic time estimate
 - 3) Most likely time estimate
 - 4) Variance of the project length

ii) Draw a network diagram from following activities. Find critical path.

Activity	A	B	C	D	E	F	G	H	I	J	K	L	M	N	O
Predecessor	-	-	-	B	B	A, E	C, D	G	H	I	C, D	C, D	C, D	J	M
Time (days)	2	2	4	6	1	1	3	45	10	7	6	2	2	1	2

[6]

