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SEAT No. :

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**P718**

**[5315] - 307**

**T.Y.B.Sc.**

**MATHEMATICS**

**MT - 337 (A) : Operations Research**

**(2013 Pattern) (Semester - III) (Paper - VII) (911A3)**

*Time : 2 Hours]*

*[Max. Marks :40*

*Instructions to the candidates:*

- 1) *All questions are compulsory.*
- 2) *Figures to the right indicate full marks.*
- 3) *Use of electronic calculator or log table is allowed.*

**Q1)** Attempt any five of the following.

**[5×2=10]**

- a) What do you mean by redundant constraint in L.P.P.?
- b) Define unit worth of a resource.
- c) Justify whether true or false: Assignment problem is a special case of transportation problem.
- d) Solve the following L.P.P.

$$\text{Maximize } z = 3x_1 + 2x_2$$

$$\text{Subject to } x_1 \leq 2, x_1, x_2 \geq 0.$$

- e) Identify the direction of increase in  $z$  of the function maximize  $Z = 2x_1 - x_2$ .
- f) Write the dual of the following L.P.P.

$$\text{Maximize } z = 2x_1 - x_2^2$$

$$\text{Subject to } x_1 + 2x_2 = 5$$

$$3x_1 + 7x_2 \leq 3$$

$$x_1, x_2 \geq 0$$

**P.T.O.**

- g) Find the initial basic feasible solution of the following transportation problem by least cost method.

|        | I  | II | III | IV | Supply |
|--------|----|----|-----|----|--------|
| A      | 10 | 30 | 20  | 13 | 5      |
| B      | 22 | 9  | 7   | 16 | 10     |
| C      | 4  | 32 | 5   | 29 | 15     |
| Demand | 5  | 5  | 10  | 10 |        |

**Q2)** Attempt Any two of the following.

**[2×5=10]**

- a) Ozark Farms uses at least 800 lb of special feed daily. The special feed is a mixture of corn and soyabean meal with the following compositions:

lb per lb of feed stuff

| Feedstuff     | Protein | Fiber | Cost (\$/lb) |
|---------------|---------|-------|--------------|
| corn          | 0.09    | 0.02  | 0.30         |
| Soyabean meal | 0.6     | 0.06  | 0.90         |

The dietary requirements of the special feed are at least 30% protein and at most 5% fiber. Formulate the problem as a linear programming 50 as to minimize the cost of the feed mix.

- b) Solve the following L.P.P. by graphical method.

Maximize  $z = 3000x + 2000y$

Subject to  $x + 2y \leq 6$

$2x + y \leq 8$

$y \leq 2$

$x - y \geq -1$

$x, y \geq 0$

- c) Solve the following L.P.P. by simplex method.

Maximize  $z = 3x_1 + 9x_2$

Subject to  $x_1 + 4x_2 \leq 8$

$x_1 + 2x_2 \leq 4$

$x_1, x_2 \geq 0.$

**Q3)** Attempt any two of the following.

**[2×5=10]**

- a) Find the optimal solution of following assignment problem. Also find alternate optional solution if it exists.

|   | I | II | III | IV | V |
|---|---|----|-----|----|---|
| A | 3 | 9  | 2   | 3  | 7 |
| B | 6 | 1  | 5   | 6  | 6 |
| C | 9 | 4  | 7   | 10 | 3 |
| D | 9 | 6  | 2   | 4  | 5 |
| E | 2 | 5  | 4   | 2  | 1 |

- b) Four operators are to be assigned to four machines. The assignment costs in dollars are given as below. Operator 1 cannot be assigned to machine C. Also operator 3 cannot be assigned to machine D. Find the optimal assignment.

|          |   | Machine |   |   |   |
|----------|---|---------|---|---|---|
|          |   | A       | B | C | D |
| Operator | 1 | 5       | 5 | — | 2 |
|          | 2 | 7       | 4 | 2 | 3 |
|          | 3 | 8       | 3 | 5 | — |
|          | 4 | 7       | 2 | 6 | 7 |

- c) Find the initial basic feasible solution of the following transportation problem by VAM.

|        | F <sub>1</sub> | F <sub>2</sub> | F <sub>3</sub> | supply |
|--------|----------------|----------------|----------------|--------|
| A      | 9              | 6              | 0              | 5      |
| B      | 5              | 1              | 0              | 20     |
| C      | 3              | 2              | 4              | 10     |
| D      | 7              | 5              | 2              | 15     |
| Demand | 25             | 10             | 15             |        |

**Q4)** Attempt any one of the following.

**[1×10=10]**

- a) Solve the following L.P.P. by Big M-method.

$$\text{Minimize } Z = 600x_1 + 500x_2$$

$$\text{Subject to } 2x_1 + x_2 \geq 80$$

$$x_1 + 2x_2 \geq 60$$

$$x_1, x_2 \geq 0.$$

- b) Find the optimal solution of the following transportation problem.

| Warehouses    | $W_1$ | $W_2$ | $W_3$ | $W_4$ | Supply |
|---------------|-------|-------|-------|-------|--------|
| $F_1$         | 1     | 2     | 1     | 4     | 30     |
| Factory $F_2$ | 3     | 3     | 2     | 1     | 50     |
| $F_3$         | 4     | 2     | 5     | 9     | 20     |
| Demand        | 20    | 40    | 30    | 10    |        |

