

Total No. of Questions : 12]

SEAT No. :

P1793

[Total No. of Pages : 5

[5059]-43

B.E. (Mech.)

COMPUTATIONAL FLUID DYNAMICS
(2008 Pattern) (Semester - II) (Elective - III)

*Time : 3 Hours]**[Max. Marks : 100**Instructions to the candidates:*

- 1) *Answer any 3 questions from each section.*
- 2) *Answers to the two sections should be written in separate books.*
- 3) *Neat diagrams must be drawn wherever necessary.*
- 4) *Figures to the right indicate full marks.*
- 5) *Use of logarithmic tables slide rule, Mollier charts, electronic pocket calculator and steam tables is allowed.*
- 6) *Assume suitable data, if necessary.*

SECTION - I

- Q1)** a) Derive the continuity equation in differential conservation form for a 3-D, unsteady, compressible flow. [12]
- b) Develop 1D, steady state convective - diffusion equation from the generalised energy equation, in partial differential form. Give the justification for cancellation of different term from the energy equation. Also write Boundary conditions. [6]

OR

- Q2)** a) Explain models of flow using control volume & state what are conservation & non-conservation form of equation. [8]
- b) What is substantial derivative? How it is different than ` derivative in differential calculus? [8]
- c) In short explain meaning of 'Divergence of velocity'? [2]

- Q3)** a) Using Taylor's series, derive the first order forward difference, backward difference and central difference approximation for the term $\frac{\partial u}{\partial y}$. [6]

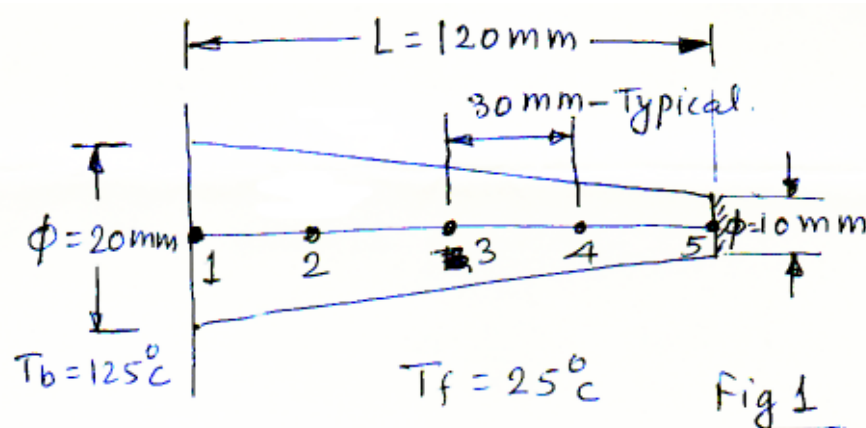
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- b) Flow between two plates can be expressed with relation $\mu \frac{\partial^2 u}{\partial y^2} = \frac{\partial P}{\partial x}$

Assuming constant, such that, $\frac{\partial^2 u}{\partial y^2} = 1$; find velocity distribution in a slit having width of 10 units and upper plate moving at a velocity of 10 units with respect to stationary lower plate. Use 5 nodes for finite differencing. Use Gauss Siedel implicit method. [10]

OR

- Q4) a)** Consider steady state heat loss through circular cross-sectioned, tapered in length, fin with temperature of the fin base and the surrounding fluid as $T_b = 125^\circ\text{C}$ and $T_f = 25^\circ\text{C}$ respectively. (Ref. fig. 1) Assume the heat loss from the end face to be negligible. Obtain temperatures of nodes 2, 3, 4, 5.



Assume $k = 1 \text{ W/mK}$ for fin material & $h = 10 \text{ W/m}^2\text{K}$ for the surrounding fluid. Derive the governing equation from the basic energy equation. Use numerical techniques. [12]

- b) What do you understand by the word 'Discretization' in reference to finite difference approach? [4]

- Q5)** Two parallel plates extended to infinity are a distance of 40mm apart. The fluid within the plates has kinematic viscosity of $2.17 \times 10^{-4} \text{ m}^2/\text{s}$ and density

of 800 kg/m^3 . The lower plate is stationary and the upper plate is suddenly set in motion in a constant velocity of 40 m/s . Find the velocity distribution within fluid in y direction for one time step (Δt). Use 5 nodes for finite differencing and apply Crank-Nicolson's implicit method. Take $\Delta t = 0.55$. Recall that the governing equation is reduced from Navier - Stokes equation and is given by

$$\rho \frac{\partial u}{\partial t} = \mu \frac{\partial^2 u}{\partial y^2} \text{ with usual notations.} \quad [16]$$

OR

- Q6)** a) What are explicit and implicit approaches used in CFD analysis? State merits and demerits of these approaches. [8]
 b) Explain Thomas Algorithm for solution of Tridiagonal matrix. Solve the following tridiagonal system with Thomas Algorithm to find T_1, T_2, T_3, T_4 . [8]

$$\begin{bmatrix} 2.04 & -1 & 0 & 0 \\ -1 & 2.04 & -1 & 0 \\ 0 & -1 & 2.04 & -1 \\ 0 & 0 & -1 & 2.04 \end{bmatrix} \times \begin{Bmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \end{Bmatrix} = \begin{Bmatrix} 40.8 \\ 0.8 \\ 0.8 \\ 200.8 \end{Bmatrix}$$

SECTION - II

- Q7)** Following 2D equation is valid over the interval

$$0 \leq x \leq 1, 0 \leq y \leq 1, t \geq 0, \frac{\partial T}{\partial t} = \frac{\partial^2 T}{\partial x^2} + \frac{\partial^2 T}{\partial y^2} \text{ Initial distribution of } T \text{ at } t = 0 \text{ is}$$

given by,

$$T(x, y, 0) = \sin(2\pi y) * \sin(2\pi x)$$

The value of T over the boundary remains at $T = 0$, for $t > 0$. Find temperature variation using $h = \frac{1}{3}$ along x and y and choosing $\Delta t = \left(\frac{1}{20}\right) \text{ s}$. Explain use of 'Alternate Direction Implicit Method' (ADI) for such problem. Find values at intermediate step i.e. $t = \left(\frac{1}{40}\right) \text{ s}$. At fixed value in y direction (i.e. j), "sweep"

in x direction to calculate T at $t = \frac{\Delta t}{2}$. [16]

OR

- Q8)** Compute the solution of the equation $\frac{\partial u}{\partial t} = -C \frac{\partial u}{\partial x}$, $C = \text{constant} > 0$, for the first two - steps, using
- Lax - Wendroff scheme
 - Mac - Cormack scheme
- With initial condition

$$u(x,0) = \begin{cases} x - x^2, & 0 \leq x \leq 1, \\ 0 & x > 1, \end{cases}$$

and boundary condition $u(0,t) = 0$ for all t , taking $\Delta x = \frac{1}{4}$ and $r = \frac{C\Delta t}{\Delta x} = \frac{1}{2}$.

[16]

- Q9)** a) Develop the solution methodology for 2D, unsteady Convection-Diffusion equation giving practice example. Explain about the possible boundary conditions. [12]
- b) What is the necessity of using upwind scheme over central difference scheme, in the solution of 1D, steady, Convection- Diffusion equation. [6]

OR

- Q10)** a) Consider a thin rod moving with a velocity 10^{-5} m/s as shown in fig2. The periphery of the rod is perfectly insulated,

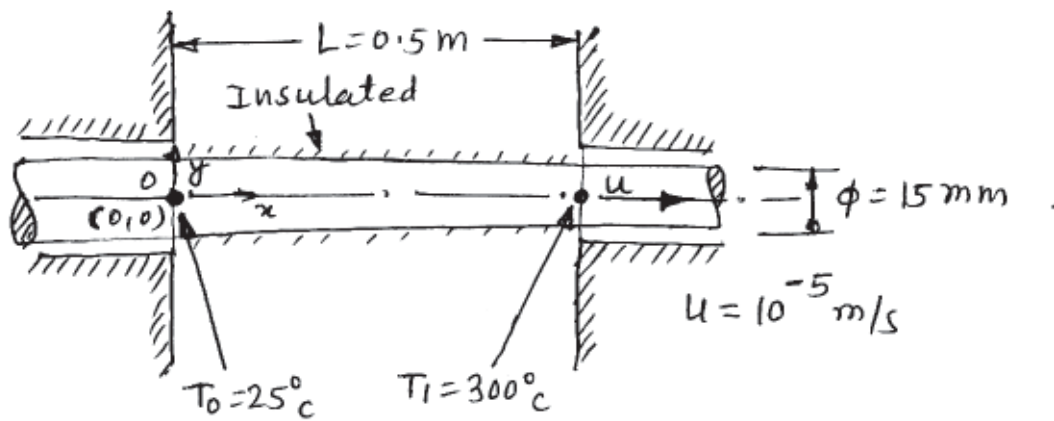


Fig 2

The rod is subjected to a specified temperature $T_0 = 25^\circ\text{C}$ for $x \leq 0$ and $T_1 = 300^\circ\text{C}$ for $x \geq L$.

Model the domain into 4 elements and find the temperature of rod at the node points. You may assume the governing equation as 1D, steady state, Convection-Diffusion equation. Solve using upwind difference approach. Derive the formulae used for finding the solution. Assume

$$\alpha = 10^{-5} \text{ m}^2/\text{s} \text{ for rod.} \quad [12]$$

- b) Give advantages and disadvantages of finite volume method. [6]

Q11)a) Why is staggered grid adopted for incompressible flows? [2]

- b) Show how the staggered grid is implemented for the pressure equation (SIMPLE). Draw the grid. [4]

- c) Present the SIMPLE algorithm and show how the pressure and velocity field is determined. [10]

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OR

Q12)a) What is difference between boundary conditions and initial conditions used in CFD. Explain about Dirichlet, Neumann and mixed boundary conditions. [8]

- b) What are the main elements involved in a complete CFD analysis? Explain these steps in detail. [8]

