Total No. of Questions—12]

[Total No. of Printed Pages-4+2

[4062]-158

# S.E. (E & TC) (Second Semester) EXAMINATION, 2011

### **ELECTROMAGNETICS**

#### (2008 PATTERN)

Time: Three Hours

Maximum Marks: 100

- N.B. :— (i) Answer Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4,
  Q. No. 5 or Q. No. 6, Q. No. 7 or Q. No. 8, Q. No. 9
  or Q. No. 10, Q. No. 11 or Q. No. 12.
  - (ii) Neat diagrams must be drawn wherever necessary.
  - (iii) Use of logarithmic tables, slide rule, Mollier charts, electronic pocket calculator and steam tables is allowed.
  - (iv) Assume suitable data, if necessary.

#### SECTION I

1. (a) State and prove Gauss law.

[6]

- (b) The spherical region 0 < r < 10 cm contains a uniform volume charge density  $\rho_{\rm V} = 4\mu{\rm C/m^3}$ . Find total charge for 0 < r < 10 cm and flux density D just outside the region. [6]
- (c) State and prove Divergence Theorem.

[6]

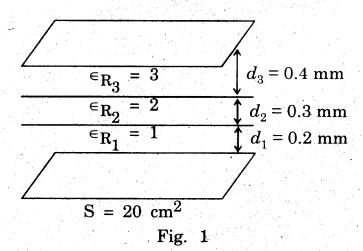
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- 2. (a) Find the flux density  $(\overline{D})$  due to uniform line charge using Gauss law. [6]
  - (b) The spherical surfaces r = 1, 2 and 3 carry surface charge densities of 20, -9 and 2 nC/m<sup>2</sup> respectively.
    - (i) How much electric flux leaves the surface r = 5?
    - (ii) Find  $\overline{D}$  at P(1, -1, 2). [6]
  - (c) An infinitely long, uniform, charge is located at y=3, z=5. If  $\rho_{\rm L}=30$  nC/m, find E at :
    - (i) the origin

(ii) 
$$P_c$$
 (5, 6, 1).

- 3. (a) Derive the expression for electric field and potential due to an electric dipole. [8]
  - (b) A parallel plate capacitor shown in the Figure 1 contains three dielectric layers as:



Find (a) Capacitance C, (b) the percentage of total stored energy located in each of the three regions. [8]

[4062]-158

- 4. (a) Given the potential field  $V = 10 y(x^3 + 5)V$ 
  - (i) Find E at the surface y = 0.
  - (ii) Show that the surface y = 0 is an equipotential surface.
  - (iii) If it is known that the surface y=0 is a conductor, find the total charge in the region 0 < x < 2, y=0, 0 < z < 1. Assume that  $\epsilon = \epsilon_0$  and that  $\delta = 0$  in the region outside the conductor.
  - (b) What is Laplace equation? Derive expression for parallel plate capacitor using Laplace's equation. [8]
- 5. (a) Find the expression for  $\overline{H}$  at any point in cylindrical coordinate system due to a filamentary conductor carrying a current I on the z-axis from  $-\infty < z < \infty$  using Biot-Savart's Law. [8]
  - (b) Given points are A(1, 2, 4), B(-2, -1, 3) and C(3, 1, -2). Let the differential current element with I = 6 A and  $|\overline{dL}|$  =  $10^{-4}$  m is located at point A. The direction of  $\overline{dL}$  is from A to B. Find  $\overline{dH}$  at C. [8]

Or

6. (a) State and explain the Stokes' theorem. Also explain the physical significance of curl. [6]

[4062]-158

3

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(b) Find the vector magnetic field intensity in Cartesian coordinates at  $P_2(1.5, 2, 3)$  caused by current filament of 24A in the  $a_z$  direction on the z-axis and extending from :

$$(i) \quad z = 0 \quad \text{to} \quad z = 6$$

$$(ii) z = 6 \text{ to } z = + \infty$$

## SECTION II

- 7. (a) Derive the boundary condition at an interface between two magnetic medium. [9]
  - (b) A unit vector directed from region 1 to region 2 at the planar boundary between two perfect dielectrics is given as:  $\overline{a}N_{12} = -(2/7)\overline{a}_x + (3/7)\overline{a}_y + (6/7)\overline{a}_z. \text{ Assume } \in_{R_1} = 3, \in_{R_2}$  $= 2 \text{ and } \overline{E}_1 = 100\overline{a}_x + 80\overline{a}_y + 60\overline{a}_z \text{ V/m}. \text{ Find } \overline{E}_2. \qquad [9]$

Or

8. (a) Region 1 is the semi-infinite space in which 2x - 5y > 0 while region 2 is defined by 2x - 5y < 0. Let  $\mu_{r_1} = 3$ ,  $\mu_{r_2} = 4$  and  $\overline{H}_1 = 30a_x$  A/m.

Find:

- (i)  $|\bar{\mathbf{B}}_1|$
- (ii)  $B_{N_1}$
- $(iii) \mid \overline{\mathbf{H}_{\mathbf{t}_1}}$

[4062]-158

(iv)  $|\overline{\mathrm{H}}_2|$  [12]

4

- (b) Derive the boundary condition for steady electric field at an interface between two perfect dielectric materials. [6]
- 9. (a) In a non-magnetic material ( $\in_R = 0$ ,  $\mu = \mu_0$ ,  $\sigma = 0$ ). Find  $\eta$ , electric field using Maxwell's equation and Poynting vector, given  $\overline{H} = 30 \cos(2\pi \times 10^8 t 6x) \overline{a}_y$ . mA/m. [8]
  - (b) What is Poynting vector? What is its significance? Derive the expression for Poynting vector V. [8]

Or

- 10. (a) Write the Maxwell equation in point form and integral for time varying fields. [4]
  - (b) A point charge of 5 cos  $10^{-7}\pi t$   $\mu$ C is located at  $P_1(0, 0, 5)$  while -5 cos  $10^7\pi t$   $\mu$ C is at  $P_2(0, 0, -15)$  both in free space. Find potential at  $P(r = 3000, \theta = 0^{\circ}, \phi = 0^{\circ})$  at t = 150 ns. [6]
  - (c) What is uniform plane wave? What is meant by transverse electromagnetic wave? [6]
- 11. (a) Explain the method of moments used to find solution of integral equation with suitable example. [10]
  - (b) Explain the procedure to draw electric field lines by numerical methods. [6]

[4062]-158

5

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- 12. (a) What is field plotting? Explain procedure to draw equipotential lines. [6]
  - (b) Consider the potential system shown in Fig. 2 set the initial values at the free nodes equal to zero and calculate the potential at free nodes for four iterations using finite difference method. [10]

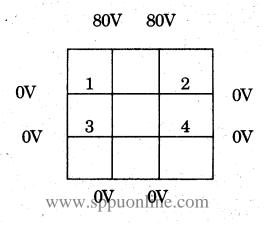


Fig. 2