Total No. of Questions—8]

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## S.E. (Comp/IT) (II Semester) EXAMINATION, 2019

## ENGINEERING MATHEMATICS—III

## (2015 **PATTERN**)

Time: Three Hours

Maximum Marks: 60

N.B. :— (i) Neat diagrams must be drawn wherever necessary.

- (ii) Figures to the right indicate full marks.
- (iii) Use of electronic pocket calculator is allowed.
- (iv) Assume suitable data, if necessary.
- **1.** (a) Solve any two differential equations: [8]

(i) 
$$\frac{d^2y}{dx^2} - 4\frac{dy}{dx} + 4y = e^{2x}\sin 4x + 2^{3x} + 6$$

(ii) 
$$x^2 \frac{d^2y}{dx^2} + x \frac{dy}{dx} - y = x^4 + 3x + 1$$

(iii)  $\frac{d^2y}{dx^2}$  + 9y = tan 3x, by using the method of variation of parameters.

(b) Solve the integral equation: [4]

$$\int_{0}^{\infty} f(x) \cos \lambda x \ dx = \begin{cases} 2 - \lambda, \ 0 \le \lambda \le 2 \\ 0, \ \lambda > 2 \end{cases}$$

P.T.O.

- 2. (a) An inductor of 0.25 henries, with negligible resistance, a capacitor of 0.04 farads are connected in series and having an alternating voltage [12 sin 6t]. Find the current and charge at any time t. [4]
  - (b) Solve any one of the following: [4]
    - (i) Obtain  $z[4^k e^{-6k}], k \ge 0$ .
    - (ii) Obtain  $z^{-1} \left[ \frac{13z}{(5z+1)(4z+1)} \right]$ .
  - (c) Solve the difference equation : [4] f(k + 2) 7f(k + 1) + 12f(k) = 0 where f(0) = 0, f(1) = 3,  $k \ge 0$ .
- 3. (a) The first four moments of a distribution about the value 5 are 2, 20, 40 and 50. Obtain the first four central moments,  $\beta_1$  and  $\beta_2$ . [4]
  - (b) Fit a straight line of the form Y = aX + b to the following data by the least square method: [4]

X	1	3	4	5	6	8
Y	-3	1	3	5	7	11

(c) A riddle is given to three students whose probabilities of solving it are  $\frac{1}{2}$ ,  $\frac{1}{3}$  and  $\frac{1}{4}$  respectively. Find the probability that the riddle is solved. [4]

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Or

4. (a) In a sample of 1,000 cases, the mean of a certain examination is 14 and standard deviation is 2.5. Assuming the distribution to be normal. Find the number of students scoring between 12 and 15.

[Given :  $Z_1 = 0.4$ ,  $A_1 = 0.1554$ ,  $Z_2 = 0.8$ ,  $A_2 = 0.2881$ ]

- (b) During working hours, on an average 3 phone calls are coming into a company within an hour. Using Poisson distribution, find the probability that during a particular working hour, there will be at the most one phone call. [4]
- (c) For a bivariate data, the regression equation of Y on X is 8x 10y = -66 and the regression equation of X on Y is 40x 18y = 214. Find the mean values of X and Y. Also, find the correlation coefficient between X and Y. [4]
- 5. (a) Find the directional derivative of  $\phi = xy^2 + yz^2 + zx^2$  at (1, 1, 1) along the line 2(x-2) = y + 1 = z 1. [4]
  - (b) Find constants a, b, c so that

$$\overline{\mathbf{F}} = (x+2y+az)\overline{i} + (bx-3y-z)\overline{j} + (4x+cy+2z)\overline{k}$$

is irrotational. [4]

(c) Find the workdone by the force

$$\overline{\mathbf{F}} = (x^2 - yz)\overline{i} + (y^2 - zx)\overline{j} + (z^2 - xy)\overline{k}$$

in taking a particle from (0, 0, 0) to (1, 2, 1). [5]

[5559]-195 3 P.T.O.

Or

- **6.** (a) Show that (any one): [4]
  - $(i) \qquad \nabla \cdot \left(\frac{\overline{a} \times \overline{r}}{r^n}\right) = 0 \qquad \qquad (ii) \qquad \nabla^2 \left[\nabla \cdot \left(\frac{\overline{r}}{r^2}\right)\right] = \frac{2}{r^4} .$
  - (b) Find the directional derivative of  $\phi = 4xz^3 3x^2y^2$  at (2, -1, 2) along the tangent to the curve

$$x = e^t \cos t$$
,  $y = e^t \sin t$ ,  $z = e^t \cot t = 0$ . [4]

- (c) Find the workdone by,  $\overline{F} = 2xy^2\overline{i} + (2x^2y + y)\overline{j}$  in taking a particle from (0, 0, 0) to (2, 4, 0) along the parabola  $y = x^2, z = 0.$  [5]
- 7. (a) Determine the analytic function f(z) = u + iv if  $u = 2x x^3 + 3xy^2$ . [4]
  - (b) Find the bilinear transformation that maps to points z = -i, 0, i into the points W = 1, 0,  $\infty$ . [4]
  - (c) Evaluate  $\int_{c} \frac{z^3}{z^2 4} dz$ , where c is the circle |z| = 3. [5]

Or

- 8. (a) Determine the analytic function f(z) = u + iv if  $u = 3x^2y + 2x^2 y^3 2y^2$ . [4]
  - (b) Find image of the circle |z 2i| = 2, under the mapping  $w = \frac{1}{2}$ .
  - (c) Evaluate  $\int_{c} \frac{2z^2 + z}{z^2 1} dz$ , where c is the circle  $|z| = \frac{3}{2} \cdot [5]$

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