

Total No. of Questions :12]

SEAT No. :

[Total No. of Pages :5

**P1667****[5058] - 155****T.E. (Computer Engg.)****THEORY OF COMPUTATION****(2008 Pattern) (Semester - I)***Time : 3 Hours]**[Max. Marks :100**Instructions to the candidates:*

- 1) *Attempt Q.1 or 2, Q.3 or 4, Q.5 or 6, Q.7 or 8, Q.9 or 10, Q.11 or 12.*
- 2) *Answer to the two sections should be written in separate books.*
- 3) *Neat diagrams must be drawn wherever necessary.*
- 4) *Figures to the right indicate full marks.*
- 5) *Assume suitable data, if necessary.*

**SECTION - I****Q1) a) Design a DFA accepting language. [8]**

$L = \{w \mid w \text{ is of the form } x01y \text{ for some strings } x \text{ and } y \text{ consisting of } 0\text{'s} \text{ and } 1\text{'s} \text{ only}\}$

**b) Design a Mealy machine that accepts strings endings with '00' and '11'. [8]****c) Define following terms with example. [2]**

- i) Symbol
- ii) Alphabet

**OR****Q2) a) Define following terms with examples. [8]**

- i) DFA
- ii) NFA
- iii) Moore Machine
- iv) Mealy Machine

***P.T.O.***

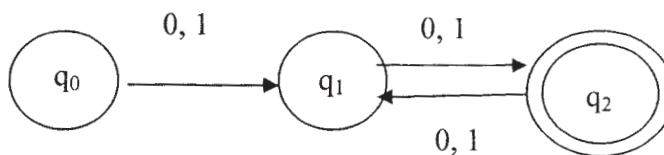
- b) Consider the following NFA with  $\epsilon$  transitions. Convert this NFA to DFA. [8]

	$\epsilon$	a	b	c
p	-	p	q	r
q	P	q	r	-
r	P	r	-	p

- c) Prove that  $(a + b)^* = (a + b)^* \cdot (a + b)^*$  [2]

- Q3)** a) Find Regular Expressions for the given sets: [8]

- The set of all strings over  $\{a, b\}$  which end in ab.
  - The set of all strings over  $\{a, b\}$  which start with ab and end with ba.
  - The set of all strings over  $\{0, 1\}$  which contains 100 as substring.
  - If  $L(r) = \{a, c, ab, cb, abb, cbb, abbb, \dots\}$  what is r?
- b) Consider the following transition diagram and convert it to its equivalent regular expression. [8]



OR

- Q4)** a) Construct a DFA for the given Regular Expression. [8]

$$(11 + 0)^* (00 + 1)^*$$

- Write a short note on Applications of Regular Expressions. [4]
- For the following regular expression, draw an FA recognizing the corresponding language.  $r = (1 + 10)^* 0$  [4]

**Q5) a)** Describe the language generated by grammars. **[8]**

$$i) \quad S \rightarrow aA / bC / b$$

$$A \rightarrow aS / bB$$

$$B \rightarrow aC / bA / a$$

$$C \rightarrow aB / bS$$

$$ii) \quad S \rightarrow bS / aA / \epsilon$$

$$A \rightarrow aA / bB / b$$

$$B \rightarrow bS$$

**b)** What do you mean by ambiguous grammar? **[8]**

Let G be a grammar:

$$S \rightarrow aB|bA$$

$$A \rightarrow a|aS|bAA$$

$$B \rightarrow b|bS|aBB$$

For the string “aaabbabbba” find:

Leftmost and Rightmost derivations.

Also draw derivation trees.

OR

**Q6) a)** Find Right Linear Grammar for given Left Linear Grammar. **[8]**

$$S \rightarrow B1|A0|C0$$

$$A \rightarrow C0|A1|B1|0$$

$$A \rightarrow B1|1$$

$$C \rightarrow A0$$

**b)** Consider the grammar G with productions. Find an equivalent grammar in CNF. **[8]**

$$S \rightarrow aB/bA$$

$$A \rightarrow a/aS/bAA$$

$$B \rightarrow b/bS/aBB$$

**SECTION - II**

- Q7)** a) Define following: [10]
- ID of PDA.
  - PDA by empty stack.
  - DPDA V/S NPDA.
  - Two stack PDA with diagram.
  - PDA by final state.
- b) Design a PDA to accept the language  $S + S * S$ . Simulate the working of above PDA for String.  $4 + 4*4$ . [8]

OR

- Q8)** a) Design a PDA to check the well formedness of paranthesis. [6]
- b) Construct PDA by null store for following grammar G. [6]

$$S \rightarrow CS1/A$$

$$A \rightarrow 1AC/S/\epsilon$$

- c) Give grammar for following PDA operations. [6]

$$\delta(q_0, o, Z) = (q_0, AZ)$$

$$\delta(q_0, 1, A) = (q_0, AA)$$

$$\delta(q_0, o, A) = (q_1, \epsilon)$$

- Q9)** a) Design a TM to accept the string which ends in 'abb' where  $L(M) = \{W \in \{a, b\}^* / W \text{ ends in } abb\}$ . Simulate with example. [8]
- b) Define following terms: [8]
- Solvability.
  - Semisolvability.
  - Unsolvability.
  - Formal difinition of T.M.

OR

**Q10)a)** Design a post machine for  $\{a^n b^{2^n} / n > 0\}$  [4]

b) Explain following: [8]

i) Programming techniques to TM.

ii) Extension to T.M.

c) Design a T.M. to accept the language  $L(M) = \{a^n b^n / n \geq 1\}$  [4]

**Q11)a)** Write short note on following: [8]

i) Post correspondence problem.

ii) Universal Turing machine

b) State the following: [8]

i) Reduction with example.

ii) Totality problem with example.

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OR

**Q12)a)** Write short note on following: [8]

i) Modified PCP problem.

ii) Recursive and recursively Enumerable language.

b) State the halting problem. Prove that halting problem of T.M. is undecidable with the help of example. [8]

