Total No. of Questions—8]

[Total No. of Printed Pages—6

Seat No.

[5057]-201

S.E. (Civil) (First Semester) EXAMINATION, 2016

ENGINEERING MATHEMATICS-III

(2012 **PATTERN**)

Time: Two Hours

Maximum Marks: 50

- N.B. :— (i) Answer Q. No. 1 or Q. No. 2, Q. No. 3 or Q. No. 4, Q. No. 5 or Q. No. 6, Q. No. 7 or Q. No. 8.
 - (ii) Figures to the right indicate full marks.
 - (iii) Non-programmable electronic pocket calculator is allowed.
 - (iv) Assume suitable data, if necessary.
 - (v) Neat diagrams must be drawn wherever necessary.
- 1. (a) Solve any two of the following:

[8]

- (i) $(D^2 4D 4)y = e^{2x} \sin 3x$
- (ii) $(x^2D^2 2xD 4) y = x^2 + 2 \log x$
- (iii) $(D^2 2D + 2) y = e^x \tan x$ (using method of variation of parameters)

P.T.O.

(b) Solve the following system of equations: [4]

$$28x + 4y - z = 32$$

$$2x + 17y + 4z = 35$$

$$x + 3y + 10z = 24$$
 by Gauss-Seidel method.

Or

- 2. (a) A 3N weight stretches a spring '15 cm'. If the weight is pulled '10 cm' below the equilibrium position and then released. Find the displacement function at any time 't'. [4]
 - (b) Solve the following system of equation of Cholesky's method: [4]

$$2x_1 - x_2 = 1$$
, $-x_1 + 3x_2 + x_3 = 0$ and $x_1 + 2x_3 = 0$

(c) Solve the following equation:

$$\frac{dy}{dx} = x - 2y,$$

using Runge-Kutta fourth order method, given that y = 1 when x = 0 and find y at x = 0. 1 taking h = 0.1. [4]

- 3. (a) The first four moments of a distribution about the values of 5 are 2, 20, 40 and 50. From the given information obtain the first four central moments, mean, standard deviation and coefficient of skewness and kurtosis.
 - (b) In a sample of 1000 cases, the mean of a certain test is '14' and standard deviation is 2.5. Assuming the distribution to be normal, find how many students score between 12 and 15 given that p(z > 0.4) = 0.1554 and p(z < -0.8) = 0.2881. [4]

[5057]-201

[4]

(c) Show that:

$$\overline{F} = (y. e^{xy}. \cos z) \hat{i} + (x. e^{xy}. \cos z) \hat{j} - (e^{xy}. \sin z) \hat{k}$$
 is irrotational. [4]

Or

- 4. (a) Attempt any one: [4]
 - (i) Show that:

$$\nabla f(r) = f'(r) \frac{\overline{r}}{r}$$

where

$$\overline{r} = x\hat{i} + y\hat{j} + z\hat{k}$$

(ii) Show that:

$$\nabla^2 \left[\frac{1}{r} \log r \right] = \frac{-1}{r^3}$$

(b) Find the directional derivative of: [4]

$$\phi = x^2 - y^2 - 2z^2$$

at the point P(2, -1, 3) in the direction of PQ where Q is (5, 6, 4).

(c) Given:

$$n = 6$$
, $\Sigma(x - 18.5) = -3$, $\Sigma(y - 50) = 0$, $\Sigma(x - 18.5)^2 = 19$, $\Sigma(y - 50)^2 = 850$, $\Sigma(x - 18.5)(y - 50) = -120$, calculate the coefficient of correlation.

[5057]-201 3 P.T.O.

5. (a) Find the work done by :

$$\overline{F} = 2xy^2 \hat{i} + (2x^2y + y) \hat{j} + xz^2 \hat{k},$$

in moving a particle from the point (0, 0, 0) to the point (2, 4, 0) along the curve $y = x^2$, z = 0. [4]

(b) Evaluate:

$$\iint\limits_{S} F \cdot d\overline{S}$$

where $\overline{F} = \frac{\overline{r}}{r^2}$ and 'S' is the surface of the sphere

$$x^2 + y^2 + z^2 = 4. ag{5}$$

(c) Evaluate: [4]

$$\iint (\nabla \times \overline{F}) \cdot d\overline{S}$$

where

$$\overline{F} = xy^2 \hat{i} + y \hat{j} + xz^2 \hat{k},$$

and 'S' is the rectangular surface bounded by :

$$x = 0, y = 0, x = 1, y = 2, z = 0.$$

Or

6. (a) Evaluate: [4]

$$\int_C (\sin y - y^3) dx + (xy^2 + x \cos y) dy,$$

using Green's theorem where 'C' is the circle :

$$x^2 + y^2 = a^2.$$

4

[5057]-201

(b) Use Gauss's Divergence theorem to evaluate: [5]

$$\iint\limits_{S} \overline{F} \cdot d\overline{S}$$

where

$$\overline{F} = vz\hat{i} + xz\hat{j} + xv\hat{k}$$

and S is the surface of sphere:

$$x^2 + y^2 + z^2 = 1$$

in the first octant.

(c) Prove that: [4]

$$\int_{C} (\overline{a} \times \overline{r}) \cdot d\overline{r} = 2 \iint_{S} \overline{a} \cdot d\overline{s}$$

$$\frac{\partial^2 y}{\partial t^2} = c^2 \frac{\partial^2 y}{\partial x^2}$$

(b) Solve: [6]

$$\frac{\partial u}{\partial t} = k \frac{\partial^2 u}{\partial x^2}$$

if:

 $(i) \ u(0, \ t) = 0$

[5057]-201 5 P.T.O.

$$(ii) \ u_x(l, \ t) = 0$$

(iii) u(x, t) is bounded and

$$(iv) \ u(x, \ 0) = \frac{u_0 \cdot x}{l}, \ 0 \le x \le l$$

Or

8. (a) A tightly streched string of length T is initially in equilibrium position is set vibrating by giving to each of its points, the velocity:

$$\left(\frac{\partial y}{\partial t}\right)_{t=0} = v_0 \sin^3\left(\frac{\pi x}{l}\right).$$

Find y(x, t) using:

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$$\partial t^2 \partial x^2$$
.

(b) An infinitely long uniform metal plate is enclosed between lines y = 0 and y = l for x > 0. The temperature is zero along the edges y = 0, y = l and at infinity. If edge x = 0 is kept at a constant temperature ' u_0 ', find the temperature distribution u(x, y).